## Homework \#1, EECS 206, F03. Due Fri. Sept. 12, by 4:30 PM

## Notes

- Review/coverage of the basic materials in Homework \#1 will occur during Monday and Wednesday lectures.
- Reading: all of "Part 1 " lecture notes.


## Skill Problems

1. [50] Concept(s): signal characteristics: energy, mean, average power, RMS value

For each of the following signals, determine the energy [3], the mean value [3], the average power [4], and the RMS value [0]. Hints: sketching the signals will help, and look at the "useful formulas" page.
(a) [0] $x_{1}(t)= \begin{cases}\cos \left(2 \pi \frac{1}{T_{0}} t\right), & t \geq 0 \\ 0, & \text { otherwise. }\end{cases}$

Answer: $\mathrm{E}\left(x_{1}\right)=\infty, \mathrm{M}\left(x_{1}\right)=0, \operatorname{MS}\left(x_{1}\right)=1 / 2, \operatorname{RMS}\left(x_{1}\right)=1 / \sqrt{2}$
(b) [10] $x_{2}(t)= \begin{cases}1, & 0<t<1 \\ 1-|t-5|, & |t-5| \leq 1 \\ 0, & \text { otherwise. }\end{cases}$
(c) [10] $x_{3}(t)=\left\{\begin{array}{ll}\cos ^{2}\left(2 \pi \frac{1}{T_{0}} t\right), & 0 \leq t \leq T_{0} \\ 0, & \text { otherwise. }\end{array}\right.$ Hint: look for $\cos ^{2}$ in the list of useful formulas.

Hint: $\operatorname{RMS}\left(x_{3}\right)=\sqrt{3 / 8}$. (But do not use this to solve for other values.)
(d) $[10] x_{4}(t)=7+3 \mathrm{e}^{-2|t|}$
(e) $[10] y_{1}[n]=\cos \left(\frac{2 \pi}{4} n\right)$
(f) $[10] y_{2}[n]= \begin{cases}1+(1 / 3)^{n}, & n \geq 0, \\ 0, & \text { otherwise }\end{cases}$
2. [20] Concept(s): signal value distributions / histograms
(a) [10] Determine the signal value distribution of signal $x[n]=\sin \left(\frac{2 \pi}{8} n\right)$.

Hint: use one period and sketch the limit as the number of histogram bins increases.
(b) [10] A discrete-time signal $x[n]$ has the following histogram.


Determine the mean value $\mathrm{M}(x)$ and standard deviation $\sigma(x)$ of this signal.
Hint: see if your values make sense in light of the center and "spread" of the histogram.
(c) [0] Determine the signal value distribution of signal $x(t)= \begin{cases}3, & |t| \leq 1 \\ -2, & 5<|t| \leq 7\end{cases}$
(Think about what happens as the number of signal samples increases, and express your singular value distribution using proportions.)
3. [20] Concept(s): periodicity, fundamental period, least common multiple

Determine whether each of the following signals is periodic, and if so, determine its fundamental period.
(a) $[0] x_{1}(t)=\cos (\sqrt{2} \pi t)$. Answer: periodic with fundamental period $T_{1}=\sqrt{2}$.
(b) [5] $x_{2}(t)=\cos (2 \pi 200 t)+\cos (2 \pi 500 t)+\cos (2 \pi 50 t)$
(c) $[5] x_{3}(t)=\cos (2 \pi 200 t)+\cos (500 t)$
(d) $[0] y_{1}[n]=\cos \left(\frac{\pi}{5} n\right)$. Answer: periodic with fundamental period $T_{1}=10$.
(e) $[0] y_{2}[n]=\cos (7 \pi n)$. Hint: sketch it! (The period is not $2 / 7$.)
(f) $[5] y_{3}[n]=\cos (\sqrt{2} \pi n)$
(g) $[5] y_{4}[n]=y_{1}[n]+y_{2}[n]$, where $y_{1}[n]$ and $y_{2}[n]$ are as defined in preceding parts.
4. [10] Concept(s): signal operations: amplitude shift/scale and time shift/scale

Consider the following signal: $x(t)= \begin{cases}1-t / 3, & |t| \leq 3 \\ 0, & \text { otherwise. }\end{cases}$
(a) [5] Sketch $y(t)=3+7 x(t / 2)$ carefully.
(b) [5] Sketch $z(t)=x\left(\frac{3-t}{2}\right)$ carefully.
5. [45] Concept(s): effects of signal operations on signal characteristics

Make a table like the following and complete it. For each entry in the table, write Y if the operation could affect the characteristic or N if it cannot. (The first column is completed for you.) If you are unsure, write "U" instead. For this problem, only your table will be graded, not your work.
Scoring: 3 points for each correct answer, 0 points for wrong answer, except 1 point for each $U$.

|  | Characteristic |  |  |  |
| :---: | :---: | :--- | :--- | :--- |
| Operation | min/max | duration | energy | mean |
| Time shift | N |  |  |  |
| Time scale | N |  |  |  |
| Time reversal | N |  |  |  |
| Amplitude shift | Y |  |  |  |
| Amplitude scale | Y |  |  |  |

6. [20] Concept(s): Using Matlab

Download the Matlab file periodic.mat, using the link on the class website just below the link to this homework set. This file contains a vector called signall that is a segment of a nearly periodic signal.
(a) [0] Start MATLAB, then load periodic.mat by typing load periodic at the Matlab prompt. (You will need to understand Matlab's "path" settings for this to work.)
(b) [5] Determine the length of the vector signal1.
(c) [5] Determine its maximum and minimum values.
(d) [10] Determine, approximately, the period of this approximately periodic discrete-time signal. Explain briefly how you determined the value.
For each part, show the Matlab command(s) that you used. (Handwritten is fine.)

## Mastery Problems

7. [25] (a) [10] Determine the mean value and average power of the signal $x_{1}(t)=a+b \cos (2 \pi f t)$.
(b) [5] Find a signal $x_{2}(t)$ that has $\mathrm{M}(x)=5$ and $\mathrm{MS}(x)=50$.
(c) [10] Find a signal $x(t)$ that has duration $=5, \mathrm{E}(x)=45$, and $\mathrm{M}(x)=3$.
8. [10] Concept(s): combining time-scaling and periodicity

Let $x(t)$ be the following continuous-time periodic signal.


Determine a period $T$ of the signal $y(t)=x(t)+x(2 t / 3-1)+x(7 t)$.
(Determining whether your answer is the fundamental period is optional.)

## Optional Extra Credit Problems

No help will be given in office hours prior to the due date for extra credit problems.
9. [10] An engineer working on a digital satellite communications system was asked by her boss to find a signal $x(t)$ that has mean value $=5$ and average power $=20$.
Should her boss take a refresher course in signal characteristics? Explain.

